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|---------------|-----|--|-----------------------------|---|---|
| 1 | (a) | | $15x^2 - 2x - 6$ | 2 | B2 for correct differentiation |
| | (b) | e.g. " $15x^2 - 2x - 6$ " = 2 oe | | 4 | (B1 for 2 of $15x^2$, $-2x$, -6 correct) |
| | | $15x^2 - 2x - 8 (= 0)$ | | | M1 ft, for equating their dy/dx to 2 |
| | | | | | M1 (dep on M1) ft their three-term quadratic |
| | | e.g. $(3x + 2)(5x - 4) (= 0)$ $x = \frac{2 \pm \sqrt{(-2)^2 - (4 \times 15 \times -8)}}{2 \times 15}$ | | | M1 for solving their quadratic equation using any correct method - if factorising, allow brackets which expanded give 2 out of 3 terms correct (if using formula or completing the square allow one sign error and some simplification – allow as far as e.g. $\frac{2 \pm \sqrt{4 + 480}}{30}$ oe) |
| | | | $-\frac{2}{3}, \frac{4}{5}$ | | A1 oe, dep on M2 (allow -0.66 or better), Both values – isw any attempt to find y coordinates |
| Total 6 marks | | | | | |

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| 2 | ai | | | | B1 tangent drawn at $P(x = 2)$ |
| | | | | | M1 (dep on B1) for a method to find gradient e.g. difference in y -values difference in x -values |
| | | | -0.6 | 3 | A1 (dep on B1) accept answers in range -0.4 to -0.7 and from correct figures for their line |
| | aii | e.g. $y = -0.6x + c$ or $y = mx + 3.6$ or $2.4 = -0.6 \times 2 + c$ | | | M1 for start of method to find the tangent equation e.g. $y = mx + c$ where m is their gradient or $y = mx + c$ where c is the y -intercept for their tangent or for substituting a point from their tangent e.g. $(2, 2.4)$ into $y = mx + c$ where m is their gradient |
| | | | $y = -0.6x + 3.6$ | 2 | A1 ft their gradient from (i) and intercept of their tangent, so long as intercept / value of c is > 3 |
| | b | | 3 | | B1 |
| | | | -1 | 2 | B1 |
| Total 7 marks | | | | | |

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| 3 | (b) | | $(-1, -15)$ | 2 | B2ft eg accept [their $-b - 4$] for the x -coordinate or [their c] for the y -coordinate (B1 ft for one correct coordinate) |
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| 4 | Line drawn at $(2, 1)$ with a positive gradient that does not intersect the curve at any other point. | | | 3 | M1 for a tangent drawn at $x = 2$ |
| | | | | | M1 (dep M1) for a correct method to work out the gradient of the tangent. |
| | | | 1.5 to 3 | | A1 for 1.5 to 3 accept answers in the range 1.5 – 3 so long as a tangent at $x = 2$ has been drawn. |
| Total 3 marks | | | | | |

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| 5 | eg $-6 = 8a + 4b - 24 + 6$ or $8a + 4b = 12$ oe | | | 6 | M1 for substituting $x = 2$ and $y = -6$ into the equation for C |
| | $\left(\frac{dy}{dx}\right) = 3ax^2 + 2bx - 12$ oe | | | | M1 at least 2 terms correct |
| | eg $16 = 12a + 4b - 12$ or $12a + 4b = 28$ oe | | | | M1ft (dep on previous M1) follow through their $\frac{dy}{dx}$ |
| | $a = 4$ and $b = -5$ | | | | M1 for $a = 4$ and $b = -5$ |
| | eg " 4 " $\times 3^3$ + " -5 " $\times 3^2 - 12 \times 3 + 6$ | | | | M1ft correctly substituting their a , their b and $x = 3$ into the equation for C |
| | | | 33 | | A1 (dep on M3) allow $(3, 33)$ |
| Total 6 marks | | | | | |

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| 6 | | | 3 | B1 | tangent drawn at $P (x = -2)$ |
| | | | | M1 | (dep on B1) for a method to find gradient eg $\frac{\text{difference in } y\text{-values}}{\text{difference in } x\text{-values}}$ or an answer in the range -0.8 to -0.2 oe |
| | Answer depends on tangent being drawn at P | 0.5 | | A1 | (dep on B1) oe accept answers in range 0.2 to 0.8 oe and from correct figures for their tangent |
| Total 3 marks | | | | | |

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| 7 | (a) | $3x^2$ or $-2 \times 2x$ or $-4x$ or -9 oe | | 2 | M1 | for differentiating one term correctly |
| | | | $3x^2 - 4x - 9$ | | A1 | for a correct expression Allow $3x^2 - 2 \times 2x - 9$ |
| | (b) | $(x =) \frac{4 \pm \sqrt{(-4)^2 - (4 \times 3 \times -9)}}{2 \times 3}$ or $3 \left[\left(x - \frac{2}{3} \right)^2 - \left(\frac{2}{3} \right)^2 \right] - 9 (= 0)$ | | 4 | M1 | for finding the critical values for a 3-term quadratic using any correct method - if using formula or completing the square allow one sign error and some simplification – allow as far as eg $\frac{4 \pm \sqrt{16 + 108}}{6}$ oe or eg $3 \left(x - \frac{2}{3} \right)^2 - 10 \frac{1}{3}$ oe) |
| | | | -1.19 and 2.52 | | A1 | for critical values of -1.19 and 2.52 or better (for this A1 mark allow -1.2 or -1.18 and 2.5 or $\frac{2 \pm \sqrt{31}}{3}$ oe) |
| | | | $x < -1.19$ | | A1 | awrt -1.19 |
| | | | $x > 2.52$ | | A1 | awrt 2.52 |
| | | | | | | Total 6 marks |

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| 8 | (a) | | 2 | M1 | for at least 2 of $12x^2$, $2x$, -20 |
| | | $12x^2 + 2x - 20$ | | A1 | |